NASA Technical Memorandum 100547

MACH NUMBER EFFECTS ON TRANSONIC AEROELASTIC FORCES AND FLUTTER CHARACTERISTICS

(NASA-TM-100547) MACH NUMEER EFFECTS ON TRANSCRIC AERGELASTIC FORCES AND FLUTTER CHARACTERISTICS (NASA) 13 p CSCL 01A

N88-16675

Unclas G3/02 0123407

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FEBRUARY 1988



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Abstract

Transonic aeroelastic stability analyses and flutter calculations are presented for a generic transport-type wing based on the use of the CAP-TSD (Computational Aeroelasticity Program - Iransonic Small Disturbance) finite-difference code. The CAP-TSD code has been recently developed for transonic unsteady aerodynamic and aeroelastic analysis of complete aircraft configurations. In this study, a binary aeroelastic system consisting of simple bending and torsion modes was used to study aeroelastic behavior at transonic speeds. Generalized aerodynamic forces are presented for a wide range of Mach number and reduced frequency. Aeroelastic characteristics are presented for variations in freestream Mach number, mass ratio, and bending-torsion frequency ratio. Flutter boundaries are presented which have two transonic dips in flutter speed. The first dip is the "usual" transonic dip involving a bending-dominated flutter mode. The second dip is characterized by a single degree-of-freedom torsion oscillation. These aeroelastic results are physically interpreted and shown to be related to the steady-state shock location and changes in generalized aerodynamic forces due to freestream Mach number.

Nomenclature

Aij	generalized aerodynamic force resulting from
,	pressure induced by mode j acting through
	displacements of mode i
AR	full-span aspect ratio
b	wing root semichord, c _r /2
С	wing local chord
Cr	wing reference chord (root chord)
Co	pressure coefficient
C ₀	critical pressure coefficient
Cr Cp Cp f(x,y)	structural mode shape
k	reduced frequency, ωc _r /2U
M	freestream Mach number
q(t)	pulse motion
q _o	pulse amplitude
Q	nondimensional dynamic pressure,
	$(U/(b\omega_{\alpha}\sqrt{\mu}))^2$
O _f	nondimensional dynamic pressure at flutter
S	Laplace transform variable, $\sigma + i\omega$
t	time, nondimensionalized by freestream speed
	and wing reference chord
t _c	nondimensional time at the pulse center
ŤŘ	wing taper ratio
Ü	freestream speed

w	constant related to the pulse width
z(x,y,t)	wing deformation at time t
αο	mean angle of attack
ή	fractional semispan
$\Lambda_{c/2}$	midchord sweep angle
μ	ratio of wing mass to mass of air in the
	truncated cone that encloses the wing
σ	damping coefficient of Laplace transform
	variable
ω	angular frequency
ωh	natural frequency of bending mode
ω_{α}	natural frequency of torsion mode

Introduction

Prediction of transonic unsteady aerodynamics for aeroelastic analysis has been aided by the development of finite-difference computer codes. An example of one of the most fully developed finite-difference codes for aeroelastic analysis is the CAP-TSD1 code recently developed at the NASA Langley Research Center. The name CAP-TSD is an acronym for Computational Aeroelasticity Program -Iransonic Small Disturbance. The code permits the calculation of steady and unsteady flows about complete aircraft configurations for aeroelastic applications in the transonic speed range. Steady and unsteady pressure comparisons were presented in Refs. 1 to 3 for numerous cases which demonstrated the geometrical applicability of CAP-TSD. These calculated results were generally in good agreement with available experimental pressure data which validated CAP-TSD for multiple component applications with mutual aerodynamic interference effects. Preliminary flutter applications of CAP-TSD were presented in Ref. 4 for a simple well-defined wing case. The calculated flutter boundaries compared well with the experimental data which gives confidence in CAP-TSD for aeroelastic prediction. More recently, the code was modified to include entropy and vorticity effects to treat cases with relatively strong shock waves.5 Without these effects, the isentropic formulation typically overpredicts the shock strength and locates the shock too far aft in comparison with experiment. The modified code includes the entropy and vorticity effects while retaining the relative simplicity and cost efficiency of the small-disturbance potential formulation. As shown in Ref. 5, the results obtained by including these effects were in very good agreement with parallel Euler calculations for attached-flow strong-shock cases.

In Refs. 1 to 5 the CAP-TSD code was shown to be accurate and efficient for transonic unsteady aerodynamic and aeroelastic applications. It is therefore timely to utilize such a computer code to study the generalized aerodynamic forces (GAFs) and aeroelastic stability characteristics of wings in transonic flow. The purpose of the paper is therefore to report on the results of a transonic unsteady

aerodynamic and aeroelastic analysis of a generic transporttype wing. The primary objectives of the research were to: (1) calculate transonic GAFs and aeroelastic characteristics for a wide range of parameter variations; and (2) correlate and physically interpret the resulting pressure distributions, GAFs, and aeroelastic stability characteristics including flutter.

In this study, a binary aeroelastic system consisting of simple bending and torsion modes was used to investigate aeroelastic behavior at transonic speeds. Results were obtained for incremental changes in freestream Mach Effects of mass ratio and bending-torsion frequency ratio on aeroelastic characteristics were also considered. The present work is analogous to the numerous aeroelastic studies performed for two-dimensional airfoils by many researchers including Isogai,6 Yang et al.,7 and Edwards, et al.8 In Refs. 6 to 8, aeroelastic analyses were performed for a large range of freestream conditions and structural parameter variations for numerous airfoil sections. These studies contributed significantly to the understanding of aeroelastic behavior at transonic Mach numbers. The present work may similarly give physical insight into the flow mechanisms which control transonic aeroelastic behavior of three-dimensional wings.

The motivations for the study were to gain a better understanding of transonic unsteady flows and aeroelastic behavior, and the need to develop efficient computational methods to predict and investigate aeroelastic phenomena. For example, the transonic GAFs in the present study were obtained by extending the pulse transfer-function analysis of Refs. 9 and 10 to treat flexible modes of motion. In this analysis, the GAFs are obtained indirectly from the response due to a smoothly varying exponentially shaped pulse. Use of the pulse transfer-function analysis gives considerable detail in the frequency domain with a significant reduction in cost over the alternative method of forced harmonic oscillation. The paper presents a description of the pulse analysis including results and comparisons which assess the capability. Transonic aeroelastic stability analyses are performed with the GAFs from the pulse analysis, using state-space aeroelastic modeling such as that reported in Refs. 11 to 14. The stability analysis of the present study is an extension of the state-space model of Refs. 13 and 14 for binary aeroelastic analysis of a three-dimensional wing. A brief description of the procedure is given in a subsequent section.

A secondary objective of the present work was to determine whether the analysis techniques are capable of predicting more challenging aeroelastic problems of significant current interest. For example, the results to be presented show a second, more critical (lower) dip in flutter speed at transonic Mach numbers slightly higher than the first dip. A flutter boundary with two transonic dips has indeed been found experimentally for a transport-type supercritical-wing flutter model tested at the NLR in the Netherlands.15 The first dip was identified in Ref. 15 as the "usual" transonic dip which involves a bending-dominated flutter mode, for the wing in predominantly attached flow. The second dip, however, occurred in a range of Mach number where the flow was separated and was identified as a torsional-buzz type of flutter, since the flutter mode was almost identical with the torsion vibration mode shape. The phenomenon was attributed in Refs. 15 and 16 to an aerodynamic resonance which occurred in a narrow range of Mach number at higher angles of attack for this wing. It has been suggested by Mabey, 17 that if this aerodynamic resonance occurs at frequencies close to wing torsional frequencies, the single degree-of-freedom torsional buzz may result. A similar torsional buzz phenomenon has also been reported by Moss and Pierce 18 where the primary torsion mode of a series of wings tended to be strongly excited under separated flow conditions. This excitation led to a sustained high-amplitude response or limit-cycle torsional buzz. In this case, a strong shock wave occurred on the upper surface of the wing, which was approximately parallel to the torsion-mode node line. Also, the shock was of fairly uniform strength across the span in the outboard region of the wing. The movement of the shock with angle of attack was such that the slope of the local pitching moment about the node line was negative rather than positive. As discussed in Refs. 17 and 18, these features seem to be necessary conditions for the occurrence of torsional buzz.

Although the current work is limited to inviscid attached flow, the results to be presented exhibit similar flutter behavior as observed in the experiments reported in Refs. 15 to 18 and described above. Certainly when strong shocks are present in the inviscid calculations or when the physical situation is known to involve separated flow, the present analysis needs to be extended to account for unmodeled effects. Nevertheless, the detailed comparisons and physical interpretations presented may give an increased understanding of unsteady transonic flows and insight into the fundamental aeroelastic mechanisms responsible for flutter at transonic speeds.

Computational Procedures

In this section, the computational procedures used in the present study are described including the CAP-TSD code, the pulse transfer-function analysis, the structural mode shapes, and the aeroelastic stability analysis.

CAP-TSD Code

The recently developed CAP-TSD1 finite-difference code was used to calculate the steady and unsteady aerodynamics presented in the paper. The CAP-TSD code is an unsteady transonic small-disturbance (TSD) code developed for transonic aeroelastic analysis of complete aircraft configurations. The code uses a time-accurate approximate factorization (AF) algorithm developed by Batina 19 for efficient solution of the unsteady TSD equation. The AF algorithm consists of a Newton linearization procedure coupled with an internal iteration technique. The CAP-TSD code is capable of treating combinations of lifting surfaces and bodies, and includes the following algorithm features: Engquist-Osher monotone differencing, (2) nonreflecting far field boundary conditions, (3) secondorder accurate spatial differencing in supersonic regions of the flow, and (4) entropy and vorticity effects to treat cases with strong shock waves. Further details of the algorithm development and solution procedures are reported in Refs. 3, 5, and 19. A detailed description of CAP-TSD may be found in Ref. 1.

Pulse Transfer-Function Analysis

Generalized aerodynamic forces which are typically used in aeroelastic analyses may be obtained by calculating several cycles of a harmonically forced oscillation with the determination of the forces based upon the last cycle of oscillation. The method of harmonic oscillation requires one flow field calculation for each value of reduced frequency of interest. By contrast, GAFs may be determined for a wide range of reduced frequency in a single flow field calculation by the pulse transfer-function analysis. 9.10 In the pulse analysis, the GAFs are computed indirectly from the response of the flow field due to a smoothly varying exponentially shaped pulse. Results computed using the pulse analysis for a pitching flat plate airfoil were first presented in Ref. 9. These results were in good agreement with parallel linear theory calculations which validated the

accuracy of the analysis. Applications to transonic airfoil cases were also in good agreement with GAFs computed using the harmonic method. Calculations for a flat plate wing undergoing a simple rigid pitching motion were presented in Ref. 10. These three-dimensional results were also shown to agree well with linear theory for reduced frequencies less than unity. Therefore, because of the computational efficiency of the pulse transfer-function analysis, the capability was extended in the present study to treat general flexible modes such as the natural vibration modes of a wing. The pulse is expressed as

$$q(t) = q_o e^{-w(t - t_c)^2}$$
 (1)

where q_0 is the pulse amplitude, w is a constant related to the width of the pulse, and t_C is the time at the center of the pulse. The deformation of any point on the wing at time t, is determined by the product of the pulse motion and the mode shape. The deformation z(x,y,t) is then given by

$$z(x,y,t) = q_o e^{-w(t-t_c)^2} f(x,y)$$
 (2)

where f(x,y) is the mode shape, and x and y are nondimensional Cartesian coordinates in the streamwise and spanwise directions, respectively. A small pulse is prescribed in a given mode of motion and the aerodynamic transients are calculated. The aerodynamic transients are then used to obtain the GAFs in the frequency domain by a transfer-function analysis. In this analysis, a fast Fourier transform (FFT) of the aerodynamic transients is divided by the FFT of the corresponding pulse motion to calculate the GAFs. The GAFs, Aij, are defined as the integrated forces resulting from pressure induced by mode j acting through the displacements of mode i. The transform assumes that the system is linear which is a valid approximation for most transonic cases, since experience has shown that the response for harmonic or aeroelastic motion is, in general, locally linear for small amplitudes of oscillation.9-14

Structural Mode Shapes

In this investigation, simple polynomial equations were assumed to describe the vibration mode shapes. The following equations simulate first bending and first torsion mode shapes of a wing, respectively:

$$f_B = y [(x - \frac{1}{2}) \sin \Lambda_{c/2} + y \cos \Lambda_{c/2}]$$
 (3)

$$f_T = y [(x - \frac{1}{2}) \cos \Lambda_{c/2} - y \sin \Lambda_{c/2}]$$
 (4)

where $\Lambda_{c/2}$ is the midchord sweep angle of the wing. The equation describing the mode shape due to bending (Eq. (3)) assumes that a node line is perpendicular to the wing midchord line at the root. The equation describing the mode shape due to torsion (Eq. (4)) assumes that a node line coincides with the wing midchord line. The amplitude of the pulse motion is selected to give a maximum tip deflection due to bending of approximately four percent of the semispan and a maximum angle of attack at the tip due to torsion of one degree.

Aeroelastic Stability Analyses

Constant sectional properties from root to tip are assumed for the aeroelastic analyses. This simplified modeling is consistent with the assumed mode shapes of Eqs. (3) and (4), which in turn assumes that the aeroelastic motion of the wing can be described by a linear combination of the fundamental bending and torsion modes. calculations were performed using state-space aeroelastic modeling such as that reported in Refs. 11 to 14. Edwards, et al.11 used a state-space model employing Pade' approximants to model the unsteady airloads and demonstrated good agreement with a time-marching technique for a linearized case. Bland and Edwards 12 demonstrated that such locally linear procedures may be used with airloads derived from a transonic smalldisturbance code for airfoil applications. Batina and Yang 13,14 used a similar procedure to study transonic aeroelastic stability and response behavior of airfoils with active controls. The stability analysis of the present study is an extension of the state-space model of Refs. 13 and 14 for binary aeroelastic analysis of a three-dimensional wing. The resulting locally linear stability model provides a relatively inexpensive determination of aeroelastic stability, while retaining the nonlinear properties of the transonic mean flow. The model is derived by assuming a linear superposition of airloads due to bending and torsion motions. The required airloads are approximated by curvefitting the CAP-TSD GAFs with a Pade' approximating function.13 The function may then be rewritten as a set of ordinary differential equations which, when coupled to the equations of motion and Laplace transformed, leads to a linear first-order matrix equation

$$\frac{s}{\omega_{\alpha}} \{z\} = [A] \{z\} \tag{5}$$

where $\{z\}$ contains the displacements, velocities, and augmented states and [A] is a real matrix of constant elements. Equation (5) is solved using linear eigenvalue solution techniques for specified values of the nondimensional dynamic pressure Q, defined as $(U/(b\omega_{\alpha}\sqrt{\mu}))^2$. The resulting eigenvalues are plotted in a dynamic pressure "root-locus" type format in the complex s-plane.

Results and Discussion

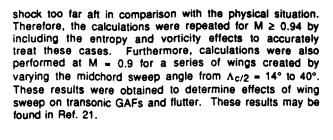
Results are first presented from the pulse transferfunction analysis to assess the accuracy and efficiency of the capability by making comparisons with other calculations. The pulse analysis was then used in a parameter study to investigate the effects of freestream Mach number on GAFs at transonic speeds. Results are also presented from the aeroelastic stability analysis, obtained using the GAFs from the pulse analysis.

Configuration Analyzed

The wing selected for the present study is the Royal Aircraft Establishment (RAE) research wing "A" that was tested in the RAE 8ft. x 6ft. transonic wind tunnel.²⁰ The wing is a structurally rigid model that has a simple planform without dihedral or twist and a symmetric RAE 101 airfoil section with a maximum thickness-to-chord ratio of 9%. As shown in Fig. 1, the wing has a midchord sweep angle of 30°, a taper ratio of one-third, and a full-span aspect ratio of six. The polynomial mode shapes that were assumed for the wing are shown in Fig. 2. The RAE

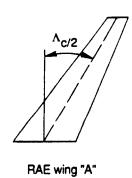
wing A is a standard configuration selected by the AGARD Fluid Dynamics Panel for steady flow calculations. Although the wing is a rigid model and no flutter data is available, the wing was selected for the present study because of the simplicity of the planform and the availability of experimental steady pressure data.²⁰ The experimental steady pressure data that is reported in Ref. 20, however, was measured with the wing mounted on an axisymmetric fuselage. Therefore, a simple fuselage was modeled with CAP-TSD, along with the wing, to allow for direct comparison with the steady pressure data. All of the other calculations to be presented were performed without the fuselage.

Calculations were performed for thirteen values of freestream Mach number including $M=0.8,\ 0.825,\ 0.85,\ 0.875,\ 0.9,\ 0.91,\ 0.92,\ 0.93,\ 0.94,\ 0.95,\ 0.96,\ 0.97,\ and 0.98. Results are presented mainly for a subset of these cases, namely at <math>M=0.8,\ 0.9,\ 0.92,\ 0.94,\ 0.96,\ and\ 0.98.$ For $M\geq0.94$, relatively strong shock waves are present in the flow. For these cases, the isentropic calculation typically overpredicts the shock strength and locates the



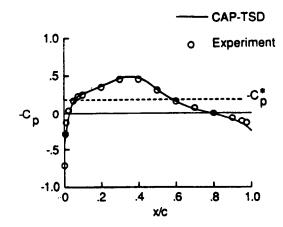
Steady Pressure Results

Steady pressure results are presented first to assess the basic character of the transonic flow. Since the unsteady flow field and hence generalized aerodynamic forces depend strongly on the transonic steady-state flow, the steady pressure distributions frequently can give physical insight into critical flow mechanisms which control aeroelastic phenomena. Of interest are the flow characteristics in the wing tip region such as the shock strength and shock location relative to the node line of the torsion mode.

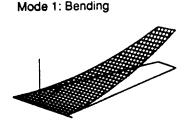


 $\Lambda_{\rm C/2}$ = 30°, AR = 6.0, TR = 1/3

Fig. 1 RAE wing "A" geometry.



(a)
$$\bar{\eta} = 0.40$$
.



Mode 2: Torsion



Fig. 2 Structural mode shapes.

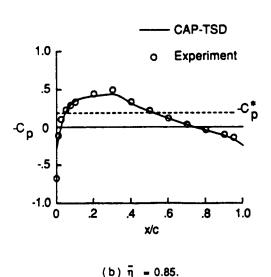


Fig. 3 Comparison between CAP-TSD and experimental steady pressure distributions on the RAE wing "A" at M = 0.90 and α_0 = 0°.

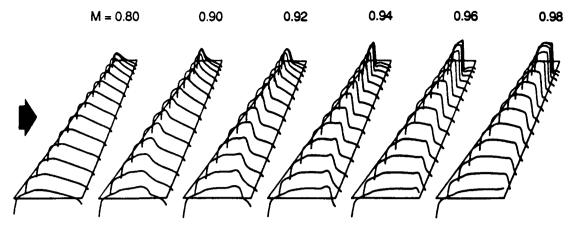


Fig. 4 Steady pressure distributions for a range of Mach number at $\alpha_0 = 0^\circ$.

Experimental Data Comparison. - To assess the accuracy of the CAP-TSD solution for this configuration, results were obtained for the RAE wing A and fuselage at M = 0.9 and α_0 = 0° for comparison with the experimental data. Steady pressure distributions at two span stations along the wing are presented in Fig. 3. Results for $\bar{\eta}$ = 0.40 are shown in Fig. 3(a); results for $\bar{\eta}$ = 0.85 are shown in Fig. 3(b). The calculated pressures are identical along the upper and lower wing surfaces, since the airfoil section is symmetric and the wing is at 0° angle of attack. These pressure distributions indicate the presence of embedded supersonic regions along the upper and lower surfaces. A mild shock wave also occurs in the inboard region of the wing (not shown). In general, the CAP-TSD pressures agree well with the experimental data.

<u>Effects of Freestream Mach Number.</u> - Steady pressure distributions at six different Mach numbers and α_0 = 0° are presented in Fig. 4. The pressures for M \geq 0.94 were computed including the entropy and vorticity corrections. At M = 0.8, the calculated pressures indicate that the flow is entirely subcritical. At M = 0.9, there is a

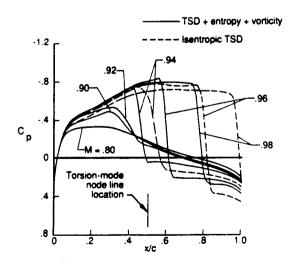


Fig. 5 Steady pressure distributions at $\bar{\eta}$ = 0.9 for a range of Mach number at α_0 = 0°.

mild shock wave in the inboard region of the wing that weakens in the outboard direction toward the wing tip. When the freestream Mach number was increased to M = 0.92 and 0.94, a moderately strong shock wave forms across the span along the upper and lower wing surfaces. In the outboard region of the wing, the shock is approximately parallel to the torsion-mode node line at the local midchord. Here the shock is also of fairly uniform strength in the spanwise direction. These features of the shock location and strength are similar to those reported in Refs. 17 and 18, which were considered to be necessary (but not sufficient) conditions for torsional buzz to occur. When the Mach number was further increased to M = 0.96 and 0.98, the shock moves aft towards the trailing edge. Since the steady pressure distributions show relatively small changes in the range $0.8 \le M \le 0.9$, it is anticipated that only small changes will occur in the GAFs. Between M = 0.92 and 0.98, much larger changes in the GAFs are expected because of the larger differences in the steady flows, especially in the wing tip region.

Figure 5 shows more detailed comparisons of the steady pressure distributions at $\bar{\eta}$ = 0.9 for the six Mach numbers ranging from M = 0.8 to 0.98. These comparisons of pressures clearly show the transonic steady flow characteristics in the wing tip region. For M ≥ 0.94, results corresponding to the calculations with and without entropy and vorticity effects are shown. Without entropy and vorticity effects, the shock is stronger and moves aft much faster with increasing Mach number. At M = 0.96 and 0.98, for example, the isentropic shock is located approximately 20% chord downstream of the nonisentropic shock. Also, at M = 0.98 the isentropic calculation predicts that the shock wave is at the trailing edge. Furthermore, the pressure distributions of Fig. 5 show that the shock wave crosses the torsion-mode node line with increasing Mach number near M = 0.94. This fact is expected to play a significant role in the aeroelastic behavior of the wing.

Generalized Aerodynamic Force Results

Generalized aerodynamic forces are presented beginning with an assessment of the accuracy and efficiency of the pulse transfer-function analysis relative to harmonic oscillation calculations. Further results are then presented from the calculations which include the nonisentropic corrections to demonstrate the effects of freestream Mach number on GAFs. All of the results are presented in the form of real and imaginary components of the GAFs, Aij, as functions of the reduced frequency k. In the present study, bending and torsion are defined as modes 1 and 2, respectively.

Linear Theory Comparison. - To assess the accuracy of the pulse transfer-function analysis to treat flexible mode shapes, results were obtained for the wing modeled as a flat plate at M = 0.9 and α_0 = 0°. These results are compared with linear theory results computed using RHOIV, an assumed pressure mode kernel function method for simple harmonic motion.22,23 The RHOIV generalized aerodynamic forces were obtained for eleven values of reduced frequency ranging from k = 0.0 to 1.0 in increments of 0.1. Comparisons of results from the pulse analysis and RHOIV are given in Fig. 6. The results shown are for the bending mode GAF due to torsion motion, A12, which is similar to wing unsteady lift-curve slope. The two sets of results are in good agreement, for the wide range of k shown, which validates the pulse analysis for application to flexible mode shapes. Results for the other three GAFs show similar good agreement between CAP-TSD and RHOIV and therefore are not shown.21

Transonic Comparison. - To assess the accuracy of the pulse analysis for transonic applications, GAFs were obtained for the wing at M = 0.9 and α_0 = 0°. The accuracy of these forces is determined by making comparisons with similar results computed using the harmonic method. Results from the harmonic method were obtained for eleven values of reduced frequency ranging from k = 0.0 to 1.0 in increments of 0.1. Comparisons of the A12 GAF calculated by the pulse analysis and the harmonic method are shown in Fig. 7. The two sets of results are in very good agreement which validates the pulse transfer-function analysis for application to transonic cases. Results for the other three GAFs show similar good agreement between the pulse analysis and the harmonic method and therefore are not shown.21

With respect to computational efficiency, the harmonic method required one flow field calculation for each value of reduced frequency for each mode of motion. This is in contrast to the pulse analysis which determined the GAFs for the entire range of frequency in a single flow field

calculation for each mode. Since eleven values of reduced frequency were selected for calculation by the harmonic method, the computational cost of obtaining the pulse results was consequently about an order of magnitude less than the cost of the harmonic method results. For the case considered here, the pulse analysis is therefore a relatively inexpensive method of determining transonic GAFs which in turn makes it economically feasible to conduct the parameter variation study reported below.

Effects of Freestream Mach Number. - To determine the effects of freestream Mach number on the GAFs, results are presented for the wing at M = 0.8, 0.9, 0.92, 0.94, 0.96, and 0.98 at zero mean angle of attack, corresponding to the steady pressure distributions presented in Figs. 4 and 5. Comparisons of GAFs at these Mach numbers are presented in Figs. 8(a) to 8(d).

For the GAFs resulting from the pressure induced by bending (A₁₁ and A₂₁ shown in Figs. 8(a) and 8(b), respectively), the real part of A21 shows the most significant change due to Mach number. With increasing Mach number, the real part of A21 decreases in magnitude for 0.92 ≤ M < 0.96. This decrease is attributed to an aft shift in the aerodynamic center which begins to occur after M = 0.92 due to the formation of the shock wave in the tip region. As shown in the steady pressure distributions of Figs. 4 and 5, there is a mild shock wave at M = 0.92 which grows in strength when the Mach number is increased to M = 0.94. Since A21 is similar to a wing moment coefficient and the torsion-mode node line is located at the local midchord, an aft shift in the aerodynamic center produces a decrease in magnitude of the real part of A21. Significant changes in aeroelastic behavior may occur for M > 0.92 because of this large decrease in magnitude of A21.

For the GAFs resulting from the pressure induced by torsion (A₁2 and A₂2 shown in Figs. 8(c) and 8(d), respectively), increasing the Mach number produced large changes in the forces especially in the low k range. These

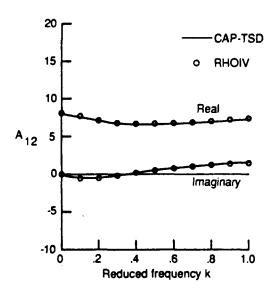


Fig. 6 Comparison between generalized aerodynamic forces calculated by CAP-TSD (linear) and RHOIV for the wing modeled as a flat plate at M=0.9 and $\alpha_0=0^\circ$.

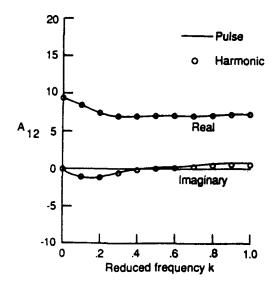
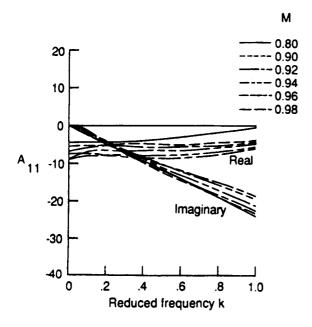
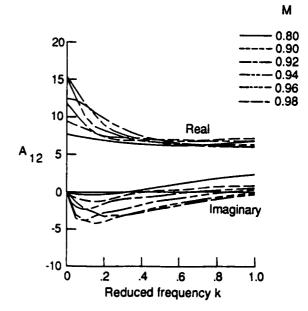
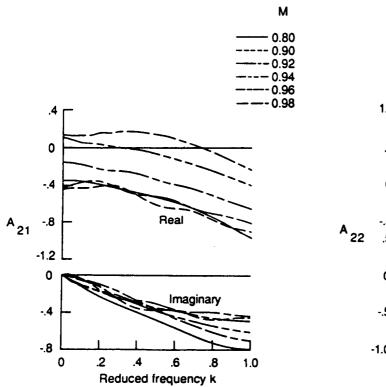


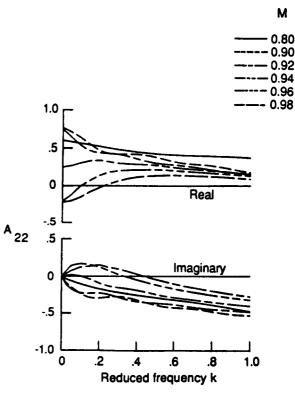
Fig. 7 Comparison between CAP-TSD generalized aerodynamic forces calculated by pulse analysis and harmonic analysis for the wing at M=0.9 and $\infty=0^{\circ}$.





- (a) GAF resulting from pressures due to bending weighted by bending displacements.
- (c) GAF resulting from pressures due to torsion weighted by bending displacements.





- (b) GAF resulting from pressures due to bending weighted by torsion displacements.
- (d) GAF resulting from pressures due to torsion weighted by torsion displacements.

Fig. 8 Comparison of generalized aerodynamic forces (GAFs) for a range of Mach number at $\alpha_0 = 0^{\circ}$.

changes in GAFs are of primary interest because they occur in the range of reduced frequency where flutter typically occurs (0.1 < k < 0.4). With increased Mach number from M = 0.8 to 0.92, for example, both the real and the imaginary parts of A₁₂ increase in magnitude. The A₁₂ force is similar to wing lift-curve slope which increases as Mach number increases. This increases both the magnitude and the phase lag of A12 which in turn controls the aeroelastic behavior for 0.8 ≤ M ≤ 0.92. As discussed by Isogai6 and later by Zwann,24 it is the increased phase lag of A12 which is the flow mechanism that produces the transonic dip in flutter speed. Also with increased Mach number, the real part of A22 generally decreases which is again attributable to an aft shift in aerodynamic center due to shock waves. Furthermore, for the higher Mach numbers in the range $0.94 \le M \le 0.98$, the imaginary part of A22 changes sign for low reduced frequencies. This change in sign indicates the possibility of single degree-of-freedom flutter in torsion.

Aeroelastic Stability and Flutter Results

Aeroelastic stability and flutter results are presented next to investigate aeroelastic characteristics at transonic speeds. Calculations were performed for several values of freestream Mach number, mass ratio, and for $\omega h/\omega_{cc} = 0.1$, 0.3, and 0.5. Root-loci plots for μ = 100 and ω_h/ω_α = 0.3 are presented in Fig. 9 for the six Mach numbers corresponding to the steady pressure distributions of Figs. 4 and 5 and the GAFs of Figs. 8(a) to 8(d). Stability results for M = 0.8, 0.9, 0.92, 0.94, 0.96, and 0.98 are shown in Figs. 9(a) through 9(f), respectively, computed including the nonisentropic corrections. The stability plots show the migration of bending and torsion root-loci as Mach number is increased. The increment in dynamic pressure shown in the figures is $\Delta Q = 0.2$. At M = 0.8, the curves indicate a classical bending-torsion type of aeroelastic behavior. Here the torsion branch moves to the left in the stable left-half

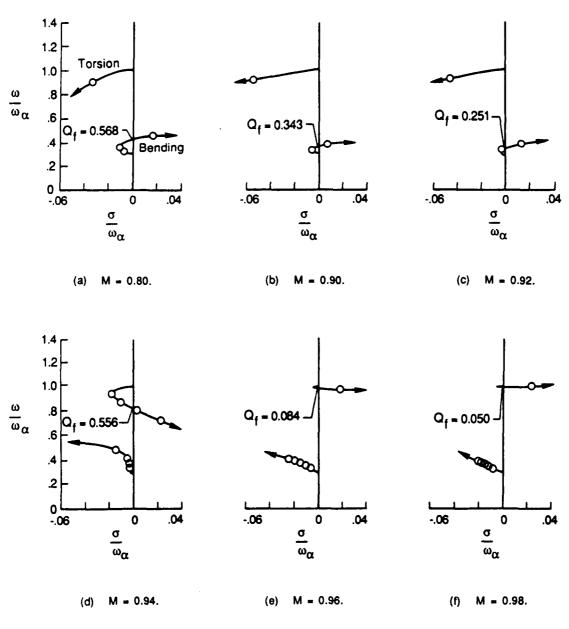
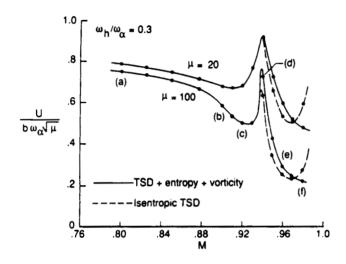
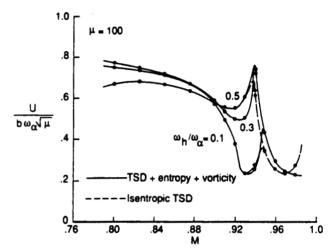


Fig. 9 Nondimensional dynamic pressure root-loci for a range of Mach number at $\alpha_0 = 0^\circ$, $\mu = 100$, $\omega_0 / \omega_0 = 0.3$, and $\Delta Q = 0.2$.

plane, with increasing dynamic pressure, while the bending-dominated branch becomes the flutter mode. With increasing Mach number in the range $0.8 \le M \le 0.92$, the flutter dynamic pressure decreases and flutter occurs at a lower frequency. Between M = 0.92 and 0.94, the root-loci coalesce in frequency and then switch, in that the flutter crossings at M = 0.94, 0.96, and 0.98 originate from the wind-off torsion mode rather than the bending mode. A rapid increase in the flutter frequency thus occurs in the range 0.92 ≤ M ≤ 0.96, from a value close to the bending natural frequency at M = 0.92 to a value close to the torsion natural frequency at M = 0.96. These aeroelastic characteristics are further explained by considering the corresponding flutter boundaries which are given in Fig. 10, and correlating these results with the steady pressures of Figs. 4 and 5, and the GAFs of Figs. 8(a) to 8(d). Figure 10(a) shows the flutter speed index (defined as $U/(b\omega_{\alpha}\sqrt{\mu})$) versus Mach number and Fig. 10(b) shows the nondimensional flutter frequency (defined as ω/ω_{α}) versus Mach number. In these figures, the points along the μ = 100 curves which are labeled (a) through (f), correspond to the root-loci of Figs. 9(a) to 9(f), respectively. Both isentropic as well as nonisentropic curves are plotted. Flutter results are also shown in Fig. 10 for μ = 20 to indicate effects due to mass ratio.

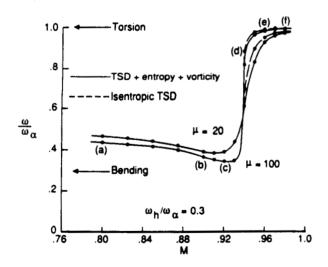
The flutter boundaries of Fig. 10(a) show two dips in flutter speed index, the second of which is deeper than the first. These transonic dips in flutter speed are deeper at the higher mass ratio of μ = 100. More specifically, as Mach number increases in the range 0.8 \leq M \leq 0.92, the flutter speed decreases as expected. This decrease is due to the

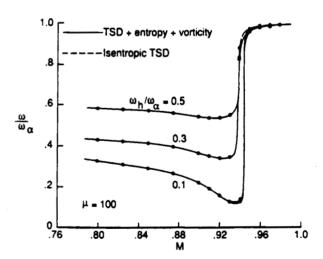




(a) flutter speed index versus Mach number.

(a) flutter speed index versus Mach number.





(b) nondimensional flutter frequency versus Mach number. (b) nondimensional flutter frequency versus Mach number.

Fig. 10 Effects of mass ratio on flutter characteristics at $\alpha_0 = 0^\circ$.

Fig. 11 Effects of bending-torsion frequency ratio on flutter characteristics at $\alpha_0 = 0^\circ$.

increased phase lag of the A₁₂ generalized aerodynamic force which occurs with increasing Mach number (Fig. 8(c)). The bottom of the first dip occurs at M = 0.91 - 0.92 for both $\mu = 20$ and 100. Here the shocks are relatively weak, and the frequency curves of Fig. 10(b) suggest that the flutter mode is predominately bending since the flutter frequency is close to the bending mode frequency. Inspection of the corresponding flutter eigenvectors confirmed this. At M = 0.92 and $\mu = 100$, for example, the ratio of the magnitudes of bending and torsion in the flutter mode eigenvector is 8:1. With a further small increase in Mach number, there is a rapid increase in flutter speed (Fig. 10(a)) which defines the "other side" of the first dip. Physically this occurs because there is a significant decrease in the magnitude of the A21 and A22 GAFs for 0.92 < M < 0.94 (Figs. 8(b) and 8(d)) due to the aft shift in aerodynamic center. Recalling that these GAFs are like moment coefficients, they decrease in magnitude when the aerodynamic center shifts aft toward the torsion-mode node line. Associated with this change in GAFs is a significant decrease in the magnitude of the imaginary part of A22 which indicates a loss of aerodynamic damping in torsion. The decrease in torsional damping causes the flutter mode to rapidly transition from a bending-dominated instability at M = 0.92 to a torsion-dominated instability at M = 0.94. This transition is shown by the rapid increase in flutter frequency from M = 0.92 to 0.94 shown in Fig. 10(b). It was also shown in Figs. 9(c) and 9(d), by the switch in root-loci, which results in a much higher frequency at the flutter crossing. Near M = 0.94, the shock, which is approximately parallel to the torsion-mode node line in the outboard region of the wing, crosses the node line with increasing Mach number. This has a destabilizing effect with respect to flutter since the damping in torsion is actually negative for low values of k as shown in Fig. 8(d). The flutter speeds in the first part of the second dip are lower in the isentropic calculations since the shock wave is stronger and located further aft of the torsion-mode node line, as previously shown in Fig. 5. The further loss of torsional damping at the higher Mach numbers produces a flutter mode that is almost identical to the torsion mode shape, as suggested by the flutter frequency values for M > 0.95 shown in Fig. 10(b). The ratio of the magnitudes of torsion and bending in the flutter eigenvector at M = 0.97 and μ = 100, for example, is 80:1. Therefore the instability in the second dip is a single degree-of-freedom flutter similar to the torsional-buzz phenomenon reported in Refs. 15 to 18. With a further increase in Mach number, the shock wave in the isentropic calculations moves aft to the trailing edge near M = 0.97, which has a stabilizing influence on the aeroelastic system since the flow about the wing is mostly supersonic. With the shock at the trailing edge, the flutter speed increases rapidly thus defining the "other side" of the second flutter dip. In the more-accurate nonisentropic calculations, however, the shock wave does not reach the trailing edge for the range of freestream Mach number Hence, the flutter characteristics are considerably different and the importance of including entropy and vorticity effects is evident.

Effects of bending-torsion frequency ratio on flutter characteristics are shown in Fig. 11. Flutter speed index and nondimensional flutter frequency as functions of freestream Mach number are shown in Figs. 11(a) and 11(b), respectively. Calculations were performed for $\omega_h/\omega_\alpha=0.1,\,0.3,\,$ and 0.5 with a mass ratio of $\mu=100.\,$ In Fig. 11, the curves for $\omega_h/\omega_\alpha=0.3$ and $\mu=100$ are the same as those shown in Fig. 10. The results indicate that the first dip in flutter speed is significantly influenced by ω_h/ω_α . With $\omega_h/\omega_\alpha=0.5,\,$ for example, the dip is very shallow in comparison to the dip with $\omega_h/\omega_\alpha=0.1.\,$ By decreasing ω_h/ω_α from 0.5 to 0.1, the flutter speed decreases by 56%. The bottom of the dip also shifts to a

slightly higher Mach number. The flutter frequency curves of Fig. 11(b) show the same trends for the three frequency ratios, each curve being shifted toward the respective bending mode frequency for M < 0.93. The flutter mode at the bottom of the first flutter dip, however, is somewhat different for the three cases. Inspection of the flutter eigenvectors revealed that the ratios of magnitudes of bending and torsion for ω_h/ω_α = 0.1, 0.3, and 0.5 are 70:1, 8:1, and 5:1, respectively. This indicates that the flutter mode at the bottom of the dip for ω_h/ω_α = 0.1 is a single degree-of-freedom bending instability. The results further indicate that the second dip in flutter speed is independent of the bending-torsion frequency ratio which is not unexpected since here the flutter mode is a single degree-of-freedom torsional instability.

Concluding Remarks

Transonic aeroelastic stability analyses and flutter calculations were presented for a generic transport-type wing based on the use of the CAP-TSD (Computational Aeroelasticity Program - Iransonic Small Disturbance) finite-difference code. In this study, a binary aeroelastic system consisting of simple bending and torsion modes was used to study aeroelastic behavior at transonic speeds. Transonic generalized aerodynamic forces (GAFs) and aeroelastic characteristics were computed for a wide range of freestream Mach number. The CAP-TSD calculations were performed by including entropy and vorticity effects to more accurately treat cases with strong shock waves.

An efficient method of calculating transonic generalized aerodynamic forces was extended to treat general flexible modes of motion of a wing. The method presented was the pulse transfer-function analysis which determines the unsteady forces indirectly from the response due to a smoothly varying exponentially shaped pulse. Comparisons of calculated GAFs for both linear and nonlinear cases showed good agreement with alternative calculations which verified the pulse analysis for application to flexible modes. Furthermore, the computational resources required by the pulse analysis were an order of magnitude less than those required by the harmonic method.

The pulse analysis was used in a parameter study to investigate the effects of freestream Mach number on GAFs at transonic speeds. The GAFs from the pulse analysis were utilized in aeroelastic stability and flutter calculations. Flutter boundaries were computed which had two transonic dips in flutter speed. The first dip was the "usual" transonic dip which involved a bending-dominated flutter mode. The second dip was characterized by a single degree-of-freedom flutter occurred at the higher Mach numbers considered due to a loss of aerodynamic damping in torsion when the steady shock location was downstream of the torsion-mode node line.

Acknowledgment

The work constitutes a part of the first author's M.S. thesis at Purdue University and was supported by the NASA Langley Graduate Aeronautics Program under grant NAG-1-372.

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National Aeronaules and Sinice Administration	Report Documentation	Page			
1. Report No.	2. Government Accession No.		3. Recipient's Catalo	g No.	
NASA TM-100547					
4. Title and Subtitle			5. Report Date		
Mach Number Effects on 1	s and	February 1988			
Flutter Characteristics		6. Performing Organization Code			
7. Author(s)		8. Performing Organization Report No.			
Ross W. Mohr, John T. Ba	tina, and Henry T. Y. Yang				
			10. Work Unit No.		
			505-63-21-01		
9. Performing Organization Name and Ad NASA Langley Research Ce			11. Contract or Grant No.		
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12. Sponsoring Agency Name and Addres			13. Type of Report and Period Covered		
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Unclassified	Inclassified		12	A02	